S3-203

B.Sc. HONS. (2nd SEMESTER) EXAMINATION, 2021 MATHEMATICS

PAPER: S-II

DIFFERENTIAL EQUATION, VECTOR CALCULUS AND ANALYSIS AND ELEMENTARY

MAX MARKS: 150

Note: Attempt all the questions.

Q.1. Solve differential equation

$$(1+x^2)\frac{dy}{dx} + 2xy = \cos x$$

Q.2. Solve

$$\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{-3x}$$

Q.3. State and prove langrange's theorem.

Q.4. If
$$r^2 = x^2 + y^2 + z^2$$
 find $grad r^n$

Q.5. A homomorphism $f=G \to G'$ is an isomorphism if and only if $\ker f = \{e\}$